

Origami⁴

Fourth International Meeting of Origami
Science, Mathematics, and Education

Robert J. Lang, editor



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